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Quarterly Progress Report #1, NAS8-20284 VIBRATION EFFECTS ON HEAT TRANSFER IN CRYOGENIC SYSTEMS

June 1, 1966 - August 31, 1966

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# Department of Mechanical Engineering Mississippi State University State College, Mississippi 39762

# Quarterly Progress Report #1, NAS8-20284 VIBRATION EFFECTS ON HEAT TRANSFER IN CRYOGENIC SYSTEMS

Period Covered: June 1, 1966 - August 31, 1966

# Ву

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# NOMENCLATURE

A	(=H'/W') Aspect ratio
a'	Maximum amplitude of vibration
B'	Body force
c¹	Specific heat
D'	Enclosure depth (see sketch below)
g'	(=a'ω <sup>(2)</sup> ) Maximum enclosure acceleration
g <sub>0</sub> '	Acceleration of gravity
H'	Enclosure height (see sketch below)
k'	Thermal conductivity
P'	Pressure
Pr	(=μ'c'/k') Prandtl number-dimensionless
Ra	$(=(T_h^{\dagger}-T_c^{\dagger})\overline{\beta}W^{\dagger}^3g/\alpha^{\dagger}v^{\dagger})$ Rayleigh number-dimensionless
T'	Temperature
T	$(=[T-T_c']/[T_h'-T_c'])$ Dimensionless temperature
t'	Time
t	(=v't'/W' <sup>2</sup> ) Dimensionless time
u'	x'-component of velocity
v'	y'-component of velocity
V'	Enclosure motion
v	$(=V'/a'\omega')$ Dimensionless enclosure motion
w'	Enclosure width (see sketch below)
x†	Cartesian coordinate (see Fig. 1)

```
(=x'/W') Dimensionless coordinate
X
y'
                Cartesian coordinate (see Fig. 1)
                (=y'/W') Dimensionless coordinate
y
\alpha^{"}
                Thermal diffusivity
B*
                Volumetric coefficient of thermal expansion
u *
                dynamic viscosity
                (=\mu'/\bar{\rho}') Kinematic viscosity
v'
ρ!
                Density
ψ'
                Stream function
                (=\psi'/\alpha') dimensionless stream function
ω1
                Frequency
Subscripts
                Vertical boundary at x' = W'
С
                Vertical Boundary at x' = 0
h
                Constant pressure
p
                Constant volume
                y direction
У
```

#### INTRODUCTION

This is the first Quarterly progress Report for NAS8-20284, VIBRATION EFFECTS ON HEAT TRANSFER IN CRYOGENIC SYSTEMS. The period covered is June 1, 1966 to August 31, 1966.

This report presents the results of an intensive search of the literature for published research on natural convection within enclosures, the effects of vibration on natural convection, and the effects of vibration on fluid transport properties (thermal conductivity and viscosity). The governing equations for the initial geometrical configuration for the natural convection study are formulated in dimensionless form and disucssed, and the final initial design of the companion experimental system is presented and discussed. A brief general discussion of the transport-property study is given.

#### ANALYSIS OF PROGRESS

The literature survey has been completed, and 225 articles have been catalogued as being of possible interest to this research. A number of these articles, which were considered most pertinent to the specific problem being investigated, were abstracted for quick reference to their content. The survey of the literature yielded a very comprehensive working bibliography covering natural convection, the effects of vibration on natural convection, and transport property determination.

An initial mathematical formulation of the following problem has been completed:

Consider the laminar two-dimensional natural convection of a fluid enclosed between two plane vertical boundaries, which are held at different temperatures, with the space between them closed by horizontal boundaries. In the remaining direction the space is considered to extend to infinity. The enclosure, formed as described above, is subjected to either longitudinal or transverse vibration.

A set of dimensionless differential equations and appropriate boundary conditions were obtained which showed that the dimensionless parameters Pr, Ra, H'/W', and  $g'/g'_0$  are sufficient to determine uniquely distributions of the stream function and temperature. The above results predict that experimentally determined heat transfer rates are correlatable by

Nu = 
$$F(Pr, Ra, H'/W', g'/g'_0)$$
.

A preliminary design of an apparatus to study experimentally the natural convection problem described in the previous paragraph has been completed. Considering force limitations of the vibration testing system, acceleration and aspect ratio limits have been established. From all possible configurations within these limits two height-depth combinations were chosen which, using three or more side plate widths each, will allow aspect ratios from 1 to 31 to be achieved. Methods have been selected for heating, cooling, temperature measurement, velocity measurement and flow visualization. Test cell final design has been

started using the guidelines above. Also, a dummy cell has been designed which is to yield information concerning induced lateral accelerations and mounting plate integrity. This information, which will be available shortly, will be of use during the final design period.

The molecular theories of liquids which appear in the literature have been studied for the purpose of selecting one theory from among those which have been proposed to use as a basis for an analytical attack on the problem of the effect of vibrations on transport properties of liquids.

#### **PROGRESS**

#### Literature Search

A literature search was made to obtain the reported research in the following areas: (a) natural convection within enclosures, (b) the effects of vibration on natural convection (both for simple shapes vibrating in an infinite atmosphere and vibrating enclosures completely or partially filled with a fluid), (c) transport property determination (both theoretical and experimental), and (d) the effects of vibration on the thermal conductivity and viscosity. The search included the following sources of information:

- 1. Engineering Index
- 2. Applied Mechanics reviews
- 3. Dissertation Abstracts
- 4. Heat Transfer Bibliography (appears periodically in International Journal of Heat Mass Transfer)

- 5. Chemical Abstracts
- 6. Science Abstracts

Appendix I is a listing of the articles located which are presented under two major categories; (a) natural convection in enclosures and the effects of vibration on natural convection and (b) transport property determination and the effects of vibrations on properties. Many of the articles have been abstracted to show the relevance of a particular article to the research problem and to serve as a reminder to the research team of the content of particular papers. Those articles not abstracted were considered to be of peripheral interest, however, each of these articles was reviewed by at least one member of the research group. It should be emphasized that Appendix I is to serve as a working bibliography, and new articles will be added as they appear or as the research proceeds and new emphasis occurs.

# The Natural Convection Problem and Its Formulation

Consider the laminar two-dimensional natural convection of a fluid enclosed between two plane parallel vertical boundaries a distance W' apart which are held at different temperatures. The space between the vertical boundaries is closed by two horizontal boundaries a distance H' apart where H'>>W'(see Fig.1). In the remaining direction, at right angles to the plane of the sketch in Fig. 1, the space is considered to extend to infinity. The enclosure, formed as described above and depicted in Fig. 1, is subjected to either longitudinal or transverse vibration.

The problem is now formulated with respect to a moving co-ordinate system which is fixed to the vibrating enclosure. Under vibratory conditions, the enclosure and confined fluid are assumed to vibrate together as a bulk, i. e., no relative motion exists between the enclosure walls and the confined liquid as a result of the vibration.

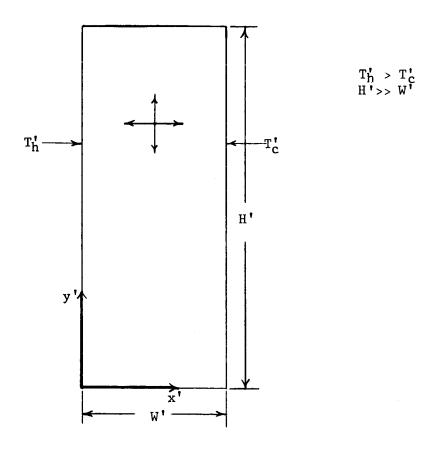


Figure 1. Schematic Diagram of Rectangular Enclosure Subjected to Either Transverse or Longitudinal Oscillations.

This assumption is crucial in that the mathematical formulation of the problem depends in large measure upon how the vibration effects are incorporated into the momentum equations. Additional assumptions relating to the manner in which density variations are considered are also required, and these assumptions must be weighed quite carefully in the final analysis. Each of the aforementioned assumptions will be discussed and justified at the point in the development where it is made.

Let  $T_h'$  and  $T_c'$  be the temperatures of the left and right vertical boundaries respectively. (All dimensional quantities are primed and all dimensionless quantities are unprimed.) Since pressure differences in the fluid will be small in comparison to the absolute pressure, variations in density will be determined by variations in the temperature T'. If the ratio  $(T_h' - T_c')/T_h'$  is small, variation in the temperature of the fluid normally needs to be considered only in the determination of the buoyancy force. However, since there is an added force in the momentum equations due to the enclosure motion, which involves the density of the fluid, and since it is of primary importance to determine the coupling of these two forces, variations in the density will also be considered in this added d'Alembert force. In the other force terms of the momentum equations the density will be considered uniform at its mean value, i.e., its value at  $\overline{T} = (T_h' + T_c')/2$ .

Considering the assumptions described above, the equation of conservation of mass is

$$\frac{\partial \mathbf{u'}}{\partial \mathbf{x'}} + \frac{\partial \mathbf{v'}}{\partial \mathbf{y'}} = 0 \tag{1}$$

where  $\mathbf{x}'$ ,  $\mathbf{y}'$  are the coordinates as shown in Fig. 1 and the corresponding velocities are  $\mathbf{u}'$ ,  $\mathbf{v}'$ .

Assuming no temperature change in the fluid due to compression and/or viscous dissipation, the energy equation becomes

$$\frac{DT'}{Dt'} = \alpha' \nabla^2 T' . \qquad (2)$$

In equation (2)  $\frac{D}{Dt}$  is the substantial derivative and  $\nabla^2$  is the Laplacian operator and are given by

$$\frac{D}{Dt'} = \frac{\partial t'}{\partial t'} + u' \frac{\partial}{\partial x'} + v' \frac{\partial}{\partial y'}$$

$$\nabla^2 = \frac{\partial^2}{\partial x^{\dagger 2}} + \frac{\partial^2}{\partial y^{\dagger 2}}$$
, and

t' is time and  $\alpha$ ' is the thermal diffusivity  $(k'/\bar{\rho}'c'_p$  for gases,  $k'/\bar{\rho}'c'_v$  for liquids where  $\bar{\rho}'$  is the density evaluated at  $\bar{T}'$ , k' is the thermal conductivity of the fluid and  $c'_p$ ,  $c'_v$  are the specific heats);  $\alpha'$  is considered uniform at its value at  $\bar{T}'$ .

Considering transverse vibration (x'direction ) the momentum equations are:

$$\frac{D\mathbf{u'}}{D\mathbf{t'}} = -\frac{1}{\overline{\rho}'} \frac{\partial P'}{\partial x'} + \nu' \nabla^2 \mathbf{u'} - \frac{\rho'}{\overline{\rho}'} \frac{dV'}{d\mathbf{t'}}$$
(3)

$$\frac{D\mathbf{v'}}{D\mathbf{t'}} = -\frac{1}{\overline{\rho}}, \quad \frac{\partial P'}{\partial \mathbf{y'}} + \mathbf{v'}\nabla^2 \mathbf{v'} + \frac{\mathbf{B''}}{\overline{\rho}}$$

where P' is the pressure in the fluid,  $\nu'$  is the kinematic viscosity  $(\frac{\mu'}{\rho'})$ , V' is the enclosure motion, and B' is the body force. B' is equal to  $-\rho'g'_0$  which, considering the previous assumption regarding the smallness of  $(T'_h - T'_c)/T'_h$ , may be written

$$B_{\mathbf{v}}^{\dagger} = -\overline{\rho}^{\dagger} g_{\mathbf{o}}^{\dagger} \overline{\beta}^{\dagger} T^{\dagger} + C$$
 (5)

where  $\overline{\beta}'$  is the volumetric coefficient of thermal expansion,  $g_0'$  is the acceleration of gravity, and C is a constant which is of no significance in that it falls out of the final equations. The enclosure motion is assumed sinusoidal so that

$$V' = a'\omega' \cos \omega't' \tag{6}$$

where a' and w' are the amplitude and frequency of vibration respectively. The last term in equation (3) is a 'so-called' d'Alembert force which arises from the vibration of the enclosure and the assumption that the enclosure and confined fluid move as a bulk.

The boundary conditions that will be placed on the variables  $u^{\:\raisebox{3.5pt}{\text{\circle*{1.5}}}}$  , and T' at the vertical boundaries are

$$u' = v' = 0$$
,  $T' = T_h'$ , at  $x' = 0$   
 $u' = v' = 0$ ,  $T' = T_C'$ , at  $x = W'$ .

The governing equations may be simplified by writing them in dimensionless form and introducing the stream function which satisfies the continuity equation identically. We define the following dimensionless variables:

$$\psi = \psi'/\alpha' \text{ where } u' = \frac{\partial \psi'}{\partial y'} \text{ and } v' = -\frac{\partial \psi}{\partial x'}$$

$$T = \frac{T' - T_C'}{T_D' - T_C'}, \quad V = \frac{V'}{a'\omega'}, \quad t = \frac{v't'}{W'^2}$$

$$x = \frac{x'}{W'}, \text{ and } y = \frac{y'}{W'}.$$

The energy equation (2) can now be written as

$$\frac{\partial T}{\partial t} + \frac{1}{Pr} \frac{\partial (T, \Psi)}{\partial (x, y)} = \frac{1}{Pr} \nabla^2 T \tag{7}$$

where

$$\frac{\partial (T, \Psi)}{\partial (x, y)} \equiv \frac{\partial T}{\partial x} \frac{\partial \Psi}{\partial y} - \frac{\partial T}{\partial y} \frac{\partial \Psi}{\partial x}$$

and Pr is the Prandtl number  $(=\frac{\mu'c'}{k'})$ . The pressure is now eliminated from equations (3) and (4),  $\rho'$  is eliminated with the use of equation (5) and equation (6) is used in writing the d'Alembert force. These operations give

$$\frac{\partial (\nabla^{2} \Psi)}{\partial t} + \frac{1}{Pr} \left\{ \frac{\partial (\nabla^{2} \Psi, \Psi)}{\partial (x, y)} \right\} = \nabla^{2} (\nabla^{2} \Psi) - Ra \left\{ \frac{\partial T}{\partial x} + \frac{g'}{g'_{O}} \sin \frac{\omega' W'^{2} t}{v'} \frac{\partial T}{\partial y} \right\} (8)$$

where Ra is the Raleigh number =  $\frac{(T_h^1 - T_c^1)\overline{B}W^{13}g}{\alpha^{1}v^{1}}$  and  $g' = a'\omega^{12}$  is the maximum acceleration of the enclosure.

The boundary conditions are now

$$\Psi(o,y,t) = \frac{\partial \Psi(o,y,t)}{\partial x} = 0 \qquad \qquad \Psi(1,y,t) = \frac{\partial \Psi(1,y,t)}{\partial x} = 0$$

$$\Psi(x,o,t) = \frac{\partial \Psi(x,o,t)}{\partial y} = 0, \qquad \qquad \Psi(x,H'/W',t) = \frac{\partial \Psi(x,H'/W',t)}{\partial y} = 0,$$

 $\Psi(x,y,o) = o$ ,  $T(x,y,o) = T_0$  (initial uniform temperature),

$$T(o,y,t) = 1, T(1,y,t) = 0, \qquad \frac{\partial T(x,o,t)}{\partial y} = \frac{\partial T(x,H'/W',t)}{\partial y} = 0.$$

For longitudinal vibrations, y' direction, equation (8) needs only to be modified by changing the sign of the last term in braces on the right-hand side to min us and the  $\frac{\partial T}{\partial y}$  to  $\frac{\partial T}{\partial x}$ . The remaining equations are unaltered.

The form of the governing equations (7) and (8) and the above boundary conditions show that the following dimensionless parameters are sufficient to determine uniquely the  $\Psi$  and T distributions: Pr, Ra, H'/W', and g'/g'. The first three parameters would appear for the same problem without vibration, and thus, this mathematical formulation shows that there is only one additional parameter required for the vibration problem, the acceleration ratio g'/g'.

From the previous discussion we see that it should be possible to express experimental heat transfer results in the following functional form:

$$Nu = F(Pr, Ra, H'/W', g'/g'_0)$$
 (9)

where Nu is an appropriately defined Nusselt number encompassing measured heat transfer rates.

# Experimental System

The initial experimental effort is to be directed toward collecting data using water as the test cell fluid. This cell will be vibrated both transversly and longitudinally, will be heated on one side by an electrical heater and cooled on the other, and will be constructed to allow flow visualization and temperature distribution measurements.

The University's 2000 pound force vibration laboratory (Unholtz-Dickie) has been readied for use on this project. The spaces have been cleared, air-conditioning installed, and instrumentation is being readied or has been ordered.

#### Test Cell Design

In the adopted nomenclature for the enclosure, an investigation has been made into the ranges of H'/W' and D'/W' which can be used. The limiting factors in the selection of test cell sizes were the test cell weight and the provision of sufficient cell depth to guarantee two-dimensionality. In order to reach the 25 g acceleration level with the vibration system to be used, a total table load of 60 pounds must not be exceeded. This total weight will consist of the heat source and sink plates, the base plate, the test fluid, and any instrumentation which must be placed on the cell. Another design objective was to study cells with aspect ratios (H'/W') from 1 to as high as 40. In order to provide as many aspect ratio configurations as possible, computer calculations were made on the size ranges available under the following assumptions.

- (1) Total cell weight of 40 pounds
- (2) One-inch thick heater, guard heater and cold plates. Assumed to be solid aluminum.
- (3) Vary H' from 2 to 24 inches in increments of 2 inches
- (4) For each H' vary W' from 1 to 30 inches in increments of 1 inch.

With these restrictive limits the ranges in available values of D'/W', H'/W' and maximum W' were calculated. Those having a D'/W' ratio of 5 or greater were assumed to satisfy two-dimensionality requirements. The cells with configurations as described are shown in Appendix 1. From these sizes two cell height-depth combinations were chosen. For each of these combinations the cell width will be varied to provide different configurations with the characteristics shown below.

Height - 16"; Depth - 7" Using 3 sets of sideplates

W'	H'/W'	D'/W'
1.7	9.3	4.1
1.0	15.8	7.0
0.5	31.0	14.0
	Height - 4"; Depth - 22" Using 4 sets of sideplates	
W'	H'/W'	D'/W'
4.0	1.0	5.5
2.0	2.0	11.0
1.0	4.0	22.0
0.5	8.0	44.0

As shown, the construction of two sets of hot and cold plates, using several sets of sideplates for each, will allow testing of a range of aspect ratios from 1 to 31. Construction and use of the 7" x 16" set of hot and cold plates will preced the construction of the 4" x 22" set. The experience of design and operation of the first cell will allow improvements in the second.

Hot, cold, and guard heater plates are to be constructed of aluminum. Hot plates and guard heaters will make use of strip heaters while the cold plate will be integrated into the evaporator circuit of a refrigeration system. All plates are to be instrumented with thermocouples in sufficient number to monitor and control the thermal environment of the cell.

Consideration, with supporting calculations, was given to electroplating the plate surfaces to provide a more uniform thermal field. The techniques of electroplating aluminum with copper or silver were such that no improvement in the thermal uniformity of the plates could be expected.

#### Temperature Measurements

The temperatures of the fluid enclosure will be measured with thermocouples imbedded in the plates. After considering several methods of measuring temperature distributions in the fluid, the following method was chosen. The factor in this selection carrying the most weight was to reduce the stirring action of any type of thermal probe during cell vibration. The optimum solution consisted of suspending butt-welded

thermocouples horizontally across the width of the cell. These thermocouples will be mounted so that they may be moved axially thus causing the junction to traverse the width of the cell. Several thermocouples of this type will be installed across the cell. A calculation was made to estimate the maximum center displacement of a thermocouple wire suspended in the above manner. The calculation indicated that a small amount of tension will be necessary in the wire in order to render this displacement negigible. The tension is to be produced by use of small spring mounts for each thermocouple.

#### Flow Visualization

Several methods of flow visualization have been reviewed and studied. One stands out in its simplicity, ease of application, and ability to yield quantitative, as well as qualitative, results. This method was described by Brooks(181a)in his thesis. It makes use of small (average size-100 microns) neutrally bouyant particles, a high intensity light source, and photographic recording equipment. The spherical shape of the particles (Eccospheres-by Emerson and Cuming, Inc.) causes them to reflect and refract light readily. The use of an interrupted light source will show the motion of the particles as traces on a photographic plate. These traces can be correlated with the frequency of light source interruption to yield velocity data. Brooks has shown that particle densities as low as 0.0083 grams/ft 3 of water are sufficient for utilization of this method; thus, no appreciable effect is expected on the motion of the fluid.

A generous supply of these particles has been ordered and the selection process is underway to obtain a satisfactory light source.

#### Design Considerations

A dummy cell, to be constructed of aluminum, has been designed to simulate the mass distribution of a typical test cell. This unit is to be instrumented with accelerometers to determine the extent of transverse vibration induced from point to point on the cell by vertical vibration of the shaker table.

This dummy unit should provide valuable information quickly on the integrity of any mounting plate designs. It will also yield estimations of the several possible modes of resonance of the test cell unit.

Considerable thought has gone into the problem of avoiding the presence of bubble coalescence. The use of distilled, filtered, and de-gassed water is anticipated. Details of the cell design are also being incorporated to eliminate any free surface and bubbles from the cell liquid.

Consideration is also being given to the possible effects of the magnetic field from the shaker on thermocouples and other instrumentation.

#### Transport Properties

The analytical study of the effect of vibrations upon the transport properties of liquids is being undertaken from the molecular (or kinetic

theory) viewpoint. Since a complete and widely accepted kinetic theory of liquids has not yet been formulated, several of the semi-empirical, approximate theories have been considered for application in this study.

The theory of Born and Green (185) is a mathematical formulation of a general kinetic theory which involves the use of a complete set of distribution functions rather than the single distribution function necessary in the kinetic theory of gases. The solution to the resulting equations is not yet known for most cases. Nevertheless, the theory of Born and Green is being considered as the basis for the study of the effect of vibrations on transport properties because of its completeness.

The theories of Eyring, Enskog and Kirkwood (204) have also been considered for this study.

In addition to selection of a theory of liquids as a basis for the analytical study, the question of the manner in which vibrational effects should be introduced into the equations has also been considered. Although no final decision has been reached on this aspect of the problem, it appears that the vibrational effects will be introduced as a sinusoidal force equally distributed among the molecules of the system.

#### PROGRESS EXPECTED DURING NEXT REPORT PERIOD

The mathematical formulation presented in this report is a first effort at obtaining the governing equations of natural convection of a fluid contained between two vertical isothermal boundaries subjected to either longitudinal or transverse oscillations. The use of a moving

coordinate system, which simplifies the writing of boundary conditions, will be explored further to ensure that all the necessary terms have been included in the momentum equations. The assumptions used in the development of the final equations (7) and (8) will be re-evaluated to ensure appropriateness and validity. Because of the complexity of the governing equations, and the lack of mathematical techniques suitable to obtain closed-form solutions of the complete equations, attempts will be made to simplify these equations to a tractable form.

Experimental work planned for accomplishment during the next reporting period will consist primarily of constructing and instrumenting a test cell. Once completed, the cell will be operated in the stationary mode and the resulting data compared with published information for natural convection in enclosures. This comparison will prove the integrity of the test cell and instrumentation configuration. With this work completed during the forthcoming report period the investigation of performance under vibration can be started in the subsequent period.

The study of the various molecular theories of liquids will be continued with the goal being the final selection of one of these theories as the basis for the study of the effects of vibrations upon the transport properties.

The criteria for final selection of a suitable theory will include: the mathematical tractability of the resulting equations, the feasibility of including an external force in the equations, and the numerical results that have been obtainable from previous applications of the theory.

APPENDIX I

**BIBLIOGRAPHY** 

# NATURAL CONVECTION IN ENCLOSURES AND THE EFFECTS OF VIBRATION ON NATURAL CONVECTION

1. ABBOT, M. R., "A Numerical Method for Solving the Equations of Natural Convection in a Narrow Concentric Cylindrical Annulus with a Horizontal Axis," Quarterly Journal of Mechanics and Applied Mathematics, 17, pp. 471-481 (1964).

A numerical method is given for solving the equations of steady laminar natural convection in a narrow concentric cylindrical annulus with a horizontal axis. Method restricted to narrow, i.e., small gap thickness, cylindrical annuli.

2. ANANTANARAYANANR. and A. RAMACHANDRAN, "Effect of Vibration on Heat Transfer from a Wire to Air in Parallel Flow," <u>Trans</u>. <u>ASME</u>, <u>80</u>, p. 1426 (1958).

This paper presents the results of an experimental investigation of the influence of vibration on heat transfer from an electrically heated nichrome wire to parallel air streams. Both frequency and amplitude increased the heat-transfer rate, in some cases up to an increase of 130%. A correlation equation is presented.

- 3. ANDRES, J. M. and U. INGARD, "Acoustical Streaming at Low Reynolds Numbers," <u>Journal of the Acoustic Society of America</u>, <u>25</u>, no. 5, pp. 932-938 (Sept. 1953).
- 4. ANDRES, J. M. and U. INGARD, "Acoustical Streaming at High Reynolds Numbers," <u>Journal of the Acoustic Society of America</u>, <u>25</u>, no. 5, pp. 923-932 (Sept. 1953).
- 5. ARPACI, V. S., J. A. CLARK and S. ESHGHY, "The Effect of Longitudinal Oscillations on Free Convection from Vertical Surfaces," <u>ASME Trans.</u>, <u>Series J. of Appl. Mechanics</u>, <u>32</u>, pp. 183-191 (March, 1965).

This is a solution for the heat transfer from a vertical surface in an infinite incompressible fluid in laminar flow being vibrated in its own plane (vertically). The solution is achieved through solution of the boundary layer equations by linearization to yield two simpler equations. Two solutions are offered; one for small frequencies by complex integration and another for large frequencies by assuming velocity and temperature profiles (Von Karman Integral technique). The results predict first a decreasing and then an increasing heat transfer coefficient as the velocity amplitude of vibration is increased. This result was verified by experiment using a vertical cylinder.

6. ASATURYAN, A. S. and B. A. TONKOSHKUROV, "Free Thermal Convection near the Linear Source of Heat," AD 610 372.

The authors consider the case of a horizontal cylinder in an infinite atmosphere. They use the boundary layer equations (question-able) and solve them using the Karman Polhausen Integral techniques. Then drawing on experiments for the limits of integration they find

$$Nu = 0.839 (Gr Pr)^{1/4}$$

There follows an experiment using nichrome wires in two oils which results in

$$Nu = 0.882 (Gr Pr)^{1/4}$$

Extensive comparison of coefficients is made with previous results.

7. BARAKAT, H.Z., "Transient Laminar Free-convection Heat and Mass Transfer in Two-dimensional Closed Containers Containing Distributed Heat Source," ASME Paper 65-WA/HT-28.

This paper makes use of finite difference techniques to determine temperature and velocity distributions in a two-dimensional rectangular container filled with a heat generating fluid. The method also allows a qualitative estimation of the transient effects. Comparison is made with the experimental results of other authors.

- 8. BATCHELOR, G. K., "Heat Convection and Buoyancy Effects in Fluids,"

  <u>Quarterly Journal Roy. Meteor Soc.</u>, <u>80</u>, no. 345, pp. 339-348, 1 plate
  (July 1954).
- 9. BATCHELOR, G. K., "Heat Transfer by Free Convection Across a Closed Cavity Between Vertical Boundaries at Different Temperatures," Quart. of Applied Mathematics, 12, pp. 209-233 (1954).

This paper presents a theoretical analysis of the two-dimensional convective motion generated by buoyancy forces on the fluid in a long rectangle, of which the two long sides are vertical boundaries held at different temperatures. No closed form analytic solution is obtained, however certain conclusions concerning when the effect of convection is negligible one made based upon fractional analysis of the governing equations.

- 10. BECK, J. V., "Calculation of Thermal Diffusivity from Temperature Measurements," J. Heat Transfer, 85, no. 2, p. 181 (1963).
- 11. BECKMAN, W., "Die Warmeubertrangung in Zylindrischen Gasschichten Bei Naturlicher Konvektion," <u>Forsh Geb. Ingenieurn</u>, <u>2</u>, pp. 165-178, 212-227, 407 (1931).

12. BERGLES A. E. and P. H. NEWELL, JR., "The Influence of Ultrasonic Vibrations on Heat Transfer to Water Flowing in Annuli," <u>Int. J. Heat and Mass Transfer</u>, 8, no. 10, pp. 1273-1280 (1965).

This paper reports the results of an experimental study of the effects of high-intensity ultrasonic vibrations on heat transfer to water flowing in annuli. The inner tube was electrically heated. Heat transfer was improved with vibration; vapor reduced the effect of vibration.

- 13. BINDER, R. C., "The Damping of Large Amplitude Vibrations of a Fluid in a Pipe," <u>Jour. of the Acoustical Soc. of America</u>, <u>15</u>, pp. 41-43 (1943).
- 14. BIRD, R. B., "Berekeningsmethoden Voor Het Warmtegeleidingsvermogen Van Gassen En Vloeistoffen," <u>Ingenieur</u>, <u>70</u>, no. 35, pp. 57-62 (Aug 29,1958).
- 15. BISHOP, E. H., L. R. MACK and J. A. SCANLAN, "Heat Transfer by Natural Convection Between Concentric Spheres," submitted to <u>International J. of Heat and Mass Transfer</u>, 1965.

An experimental investigation is described concerning natural convection of air enclosed between two isothermal concentric spheres of various diameter ratios. Measured temperature profiles are analyzed in detail. The profiles are explained in terms of the flow patterns observed in the visual study. An emperical equation is presented that correlates the measured heat transfer rates to within 15%.

16. BISHOP, E. H., R. S. KOLFLAT, L. R. MACK and J. A. SCANLAN, "Convective Heat Transfer Between Concentric Spheres," <u>Proc. 1964 Heat Transfer Fluid Mech. Inst.</u>, pp. 69-80, Standford Univ. Press (1964).

This paper presents the result of a study of the flow patterns and temperature distributions occuring between two concentric isothermal spheres of various diameter ratios with air in the intervening space. Qualitative descriptions and photographs of the flow patterns are given and temperature distributions are correlated with these patterns.

- 17. BISHOP, E. H., R. S. KOLFLAT, L. R. MACK, and J. A. SCANLAN, "Photographic Studies of Convection Patterns between Concentric Spheres,"

  <u>Soc. Photo-optical Instr. Engages.</u> J., <u>3</u>, pp. 47-49 (1964-1965).
- 18. BJORKLUND, I. S., and W. M. KAYS, <u>Trans. ASME J. Heat Transfer</u>, <u>81</u>, Series C, 175 (1959). Concerns heat convection in air enclosed by two rotating cylinders.
- 19. BLANKENSHIP, V. D., "The Influence of Transverse Harmonic Oscillations on the Heat Transfer from Finite and Infinite Vertical Plates in Free Convection," PhD thesis Univ. of Michigan, Ann Arbor (August 1962).

20. BLANKENSHIP, V. D. and J. A. CLARK, "Experimental Effects of Transverse Oscillations on Free Convection of a Vertical, Finite Plate," <u>Trans. Amer. Soc. Mech. Engrs. Series C, Journal of Heat Transfer, 86</u>, 2, pp. 159-165 (May 1964).

The authors present an analytical solution to the problem of predicting the effects of transverse oscillation on free convection from a vertical finite plate. The Formulation of the problem assumes that the bouyancy effects predominate, the fluid is incompressible, the bulk fluid moves as a mass, and that the normal boundary layer assumptions are appropriate for this problem. They consider that the effects of the effects of oscillations result mainly from an oscillating potential flow at the outer edge of the boundary layer. The method of solution employs a pertubation technique where the flow is considered to be principally nonvibratory free convection with velocity oscillations imposed as perturbations. The zeroth order approximation is taken as Ostrach's solution to the same problem without oscillations. The solution predicts a small decrease in the heat transfer rate for laminar flow. This conclusion was confirmed by experiment.

21. BLANKENSHIP, V. D. and J. A. CLARK, "Effects of Oscillation from a Vertical, Finite Plate," <u>Trans. Amer. Soc. Engages.</u>, <u>Series C, J. of Heat Transfer</u>, <u>86</u>, no. 2, pp. 149-158 (May, 1964).

This paper presents the results of experiments performed to confirm the conclusions reached analytically and reported in another paper. For laminar flow it was found that there was a negligible small reduction in the heat transfer rate as was predicted analytically. In addition, smoke traces indicated that for certain oscillation frequencies and amplitudes there was an early transition from laminar to turbulent flow with accompanying increases in the heat transfer rate. There is some question as to the accuracy of the experimental apparatus in obtaining true transverse oscillations of the plate. It appears that the method used to connect the plate to the exciter could permit a considerable amount of cross talk.

- 22. BOELTER, L. M. K. and W. E. MASON, "Vibration--its effect on Heat Transfer," <u>Power Plant Engng.</u>, <u>44</u>, pp. 43-46 (1940).
- 23. BOGGS, J. H. and W. L. SIBBITT, "Thermal Conductivity Meas. of Viscous Liquids," <u>Indust. Engng. Chem.</u>, <u>47</u>, 2, 289-293 (Feb. 1955).
- 24. BOLOTINA, K. S., "On Usloviyakh Vozniknoveniya Svobodnoi Knoveksii V Kanale Pryamougol'nogo Secheniyq," Akademiya Wauk SSSR, Izvestiya, Otdelenie Teknicheskikh Nauk, Mekhanika i Mashinostreonie, no. 1, pp. 73-6 (Jan-Feb 1962). (Conditions involving free convection in Tectangular channel, asympotic solution presented for passage from molecular heat transfer to free convection in vertical rectangular channel.)

- 25. BORISOV, YU. YA. and YU. G. STATNIKOV, "Flow Currents Generated in an Acoustic Standing Wave," <u>Jour. of Acoustics (USSR)</u> Vol. <u>11</u>, no. 1, (Jan-Mar 1965).
- 26. BUGAENKO, G. A., "Free Thermal Convection in Vertical Cylinders of Arbitrary Cross Sections," (in Russian) Pril. Mat. Mekh., 17, no. 4, pp. 496-500 (July-Aug. 1953).
- 27. BURDOKOV, A. P. and NAKORIZKOV, V. E., "Heat Transfer from a Cylinder in a Sound Field at Grashof numbers tending to Zero," <u>Teploobmen at Tsilindra v Zvukovom Pole pri Priklandoi nekhaniki I Teknicheskoi Fiziki</u>, pp. 119-124 (Jan/Feb. 1965). (in Russian)
- 28. BYKOV, L. T., "Estimation of the Rate of Displacement of Air in a Confined Space with Natural Convection," <u>Jour. of Engineering Physics</u> (Russian) <u>8</u>, no. 2 (Feb. 1965).
- 29. BYKOV, L. T. and V. V. MALOZEMOV, "Some Temperature Distribution Relations for Confined Spaces with Internal Heat Sources," <u>Jour. of Engr. Physics</u> (Russian), <u>8</u>, no. 2 (Feb. 1965).
- 30. CARLSON, W. O., "Interferometric Studies of Convective Flow Phenomena in Vertical Plane Enclosed Air Layers," PhD Thesis, Graduate School, Univ. of Minn. (1956).
- 31. CAVALLARO, L., A. INCELLI and G. PANCALDI, "On Some Improvements on a Cryoscopic Precision Apparatus and on the Control of a Thermocouple," (in Italian) <u>Ric. Sci.</u>, <u>23</u>, no. 12, pp. 2237-2243 (Dec. 1953).
- 32. CHANDRASEKHAR, S., <u>Proc. Roy. Soc.</u> (London) <u>A237</u>, p. 476 (1956). Free convection in thin layers heated from below.
- 33. CHERVIAKOV, S. S., "Experimental Investigation of the Influence of Vibration of a Sphere on Heat and Mass Exchange in a Turbulent Stream of Air," <u>In Its J. of Eng. Phys. Misk</u>, 6, no. 6, pp. 27034 (June 1963, 17 Dec. 1963). See N64-11965 03=01 OTS \$3.50.
- 34. CHERVIAKOV, S. S., "Experimental Investigation of the Effect of Vibrations on the Heat and Mass Transfer of a Cylinder and a Cone in Turbulent Air Flow," <u>Inzhenerno-Fizicheskii Zhurnal</u>, 6, pp. 10-21 (Aug. 1963). (in Russian)
- 35. COULBERT, C. D., "Mach-Zehnder Interferometer Applications as Used in the Study of Convection and Conduction Heat-Transfer Systems," <u>ASME Annual Meeting</u>, <u>New York</u>, (Dec. 1952) Paper No. 52-A-9, 3 pp. 13 figs.

- 36. CRANDALL, I. B., "Theory of Vibrating Systems and Sound," D. Van Nostrand, Co., Inc., New York, pp. 95-103 and 229-241 (1927).
- 37. CRAWFORD, L. and R. LEMLICH, "Natural Convection in Horizontal Concentric Cylindrical Annuli," <u>Industiral and Engage</u>. <u>Chemistry Fundamentals</u>, 1, qp. 260-264 (1962).

The problem of steady, laminar natural convection between horizontal concentric cylinders was attacked numerically via finite difference approximations to the governing equations. The stream function and temperature distribution were obtained for several diameter ratios and Grashof numbers. No unstable flow conditions were obtained, but such conditions have been shown to exist by other researchers. An analytical solution is given for the creeping flow case, which is of little importance in most applications.

- 38. DE GRAFF, J. G. A. and E. F. M. VAN DER HELD, "The Realtion Between the Heat Transfer and the Convection Phenomena in Enclosed Plane Layers," <u>Appl. Sci. Res.</u> (A), <u>3</u>, no. 6, pp. 393-409 (1953).
- 39. DEAVER, F. K., W. R. PENNEY, and T. B. JEFFERSON, "Heat Transfer from an Oscillating Horizontal Wire to Water," <u>Trans. Amer. Soc. Mech. Engng. Series C</u>, <u>Journal of Heat transfer</u>, <u>84</u>, pp. 251-256 (1962).

A small horizontal wire in water was vibrated at low frequencies and relatively large amplitudes and the effects of this vibration on the heat flux were experimentally determined. It was concluded that either forced, free, or mixed convection correlations could be used to predict the heat transfer coefficient depending on the relative values of the Reynolds number and the Rayleigh number. The Reynolds number is based upon the mean velocity of the wire. In the mixed convection regime a correlation (conservative) was proposed.

- 40. DECKER, A. S., "Natural Convection Equipment," <u>ASHRAE</u>, <u>J</u> 7, no. 4, p. 45 (1965).
- 41. DONALDSON, I. G., "Free Convection in a Vertical Tube with a Linear Wall Temperature Gradient," <u>Austral</u>. <u>J</u>. <u>Phys.</u>, <u>14</u>, p. 529 (1961).

This paper presents a theoretical analysis of convection in a vertical tube closed at both ends in which the temperature of the walls is arranged to increase linearly with depth. An experimental study showed good agreement with theory up to a certain value of a modified Rayleigh number.

42. DOUGALL, R. S., T. CHIANG and R. M. FAND, "A study of the Differential Equations of Coupled Vibrations and Free Convection from a Heated Horizontal Cylinder," Wright-Patterson, AFB, Ohio, Aeronautical Research Lab, p. 24, 46, (Dec. 1961). refs. ARL-148 Part I.

- 43. DRAKHLIN, E., "On Heat Convection in a Spherical Cavity," (in Russian), Zh. Tekh. Fiz., 22, no. 5, pp. 829-831 (May 1952).
- 44. DROPKIN, D. and SOMERSCALES, E., "Heat Transfer by Natural Convection in Liquids Confined by Two Parallel Plates which are Inclined at Various Angles with Respect to the Horizontal," <u>Journal of Heat Transfer C 87</u>, pp. 77-84 (1965).

This paper is concerned with the effect of inclination on natural convection heat transfer in liquids confined by two parallel plates. Data is taken and mathematical relations are developed from which heat transfer coefficients can be determined. The fluids used were water, silicon oils, and mercury. One point of interest is that the authors considered the effect of aspect ratio negligible.

45. DUSINBERRE, G. M., "A Note On the Implicit Method for Finite-Difference Heat Transfer Calculations," <u>ASME Trans.</u>, <u>J. Heat transfer</u>, <u>Series C</u>, pp. 94-95 (Feb. 1961).

This paper states that the advantage of the implicit method is the possibility of using large time intervals. However, after considering a particular problem it is concluded that the advantage of the larger time intervals may be outweighed by the loss of accuracy and the need for a longer computation time.

- 46. ECKART, C., "Vortices and Streams Caused by Sound Waves," The Physical Review, 73, no. 1, pp. 68-76 (Jan. 1, 1948).
- 47. ECKERT, E. R. G. and W. O. CARLSON, "Natural Convection in Air Layer Enclosed Between Two Vertical Plates with Different Temperatures," <u>Inter. J. of Heat and Mass Transfer</u>, 2, pp. 106-120 (1961).

Presents experimental technique, data, and correlations for parallel vertical flat plates using air. No vibration. Interferometry used to determine temperature profiles. Aspect ratios reported are 2.5, 10, 20 and 46.67. Relations for local and average heat transfer are given.

48. EICHHORN, R., "Flow Visualization and Velocity Meas. in Natural Conv. with Tellurium Die Method," ASME Trans., J. Heat Transfer, 83, Series C, pp. 379-381.

A technical brief which describes the use of tellurium probes to visualize the natural convective flows within various geometrical configurations. Requires an electrolyte solution.

49. EICHHORN, R., "Measurement of Low Speed Gas Flows by Partical Trajectories: A New Determination of Free Convection Velocity Profiles,"

Int. J. Heat Mass Transfer, 5, p. 915 (1962).

Concerns heat transfer data for a heated horizontal wire immersed in a water bath and oscillating in a vertical plane. This paper describes a technique of measuring air velocities in free convection flows using dust (zinc sterate) particles for tracers and photographic plates. The method agreed closely with the analytical solution except at points outside the maximum velocity area. Random air currents and very precise control of illumination make the method a tedious one.

50. ELDER, J. W., "Laminar Free convection in a Vertical Slot," <u>J. Fluid Mech.</u> 23, Pat. I, pp. 77-98 (1965).

This is an experimental study of the interaction of the shear and buoyancy forces in natural convection in a liquid. The experimental apparatus was a rectangular slot with two isothermal opposing sides at different temperatures. The experiments were run using medicinal paraffin and a silicone oil and were restricted to aspect ratios from 1 to 60 and Rayleigh numbers from 10 to  $10^8$ .

The major emphasis in this report is placed on the uniform vertical temperature gradient found in the interior of the flow for Rayleigh numbers greater than  $10^4$  and the mechanics of the secondary flows.

51. ELDER, J. W., "Turbulent Free Convection in a Vertical Slot," <u>J. Fluid Mech.</u> 23, Part I, pp. 99-111 (1965).

An experimental study of unsteady and turbulent free convective flow in a vertical slot across which these is a uniform temperature difference. The aspect ratio was in the range 10--30, while the value of the Rayleigh number was greater than  $10^6$ . Using flow visualization techniques, the flow pattern in the slot was shown to consist of two trains of breaking waves, one travelling up the hot wall and one travelling down the cold wall, inducing a turbulent zone in the central portion of the interior. Within the interior of the slot, between the mixing regions near the walls, there existed a uniform mean temperature field.

52. EMERY, A. and CHU, N. C., "Heat Transfer Across Vertical Layers," <u>J. of Heat Transfer</u>, <u>c</u> 87, pp. 110-116 (1965).

Vertical surfaces were maintained at different constant temperatures. Various fluids giving a Prandtl number of from 3 to 30,000 were tested. Analytical approach considered boundary layer approximations coupled with integral techniques-solution very limited even though experiment and theory were reasonable close. An empircal equation is given that correlates the experimental results and contains the height to thickness ratio of the layer. This equation does not correspond to those given by other researchers.

53. ESHGHY, S., V. S. ARPACI, and J. A. CLARK, "The Effect of Longitudinal Oscillations on Fluid flow and Heat Transfer from Vertical Surfaces in Free Convection". Paper in preparation, also Tech. Report no. 1, DRA Project 05065, Univ. of Michigan, Ann Arbor, June, 1963.

54. FAND, R. M. and KAYE, J., "Influence of Sound on Free Convection from Horizontal Cylinder," <u>ASME Trans. J. Heat Transfer</u>, <u>83</u>, Series C, no.2, pp. 133-48 (May 1961).

Reports resulted of flow visualization studies of flow field about horizontal heated cylinder for several sound pressure levels, frequencies and 1/d ratios. Concludes that vortex motion begins to form in flow field at a "critical sound pressure level," and becomes fully developed at a higher SPL. Later paper by same authors contains essentially this information with improved discussion.

- 55. FAND, R. M. and J. KAYE, "Effects of High Intensity Stationary & Progressive Sound Fields on Free Convection from a Horizontal Cylinder,"

  TN 59-18 (1959).
- 56. FAND, R. M. and J. KAYE, "The Influence of Vertical Vibration on Heat Transfer in Free Convection from a Horizontal Cylinder," <u>Intern. Dev. in Heat Transfer</u>, pp. 490-498, ASME (1961).

A 'critical' intensity of vibration (amplitude x frequency) was determined below which the influence of the vibration upon the heat transfer rate was negligible and above which the effect increased the heat flux significantly. This critical intensity was reported to be 0.3 ft./sec. Flow studies indicated that the significant rise in heat flux for intensities of vibration greater than 0.3 ft./sec. was due to vibrationally induced turbulence. The turbulence observed was not-similar to that resulting from transverse vibration induced by a sound field. Empirical equations are presented for the heat flux. The general conclusions reached are that the effects of vibration upon the heat flux must be taken into account and that the direction of the vibration vector relative to the direction of the gravity force controls the basic character of the flow.

57. FAND, R.M. and J. KAYE, "Acoustic Streaming Near a Heated Cylinder," <u>Journal of Acoustical Soc. of America</u>, 32, p. 579 (1960).

This paper reports the results of an experimental investigation of the influence of intense acoustic vibrations on the rate of heat transfer from a circular cylinder to air in crossflow. An excellent review of the literature concerning the effects of vibrations, induced by sound fields and mechanically, on natural convection from a simple shape to an infinite atmosphere is given.

- 58. FAND, R. M. and J. KAYE, "The Influence of Sound on Free Convection from a Horizontal Cylinder," ASME Paper No. 60-HT-14.
- 59. FAND, R. M., "On the Mechanism of Interaction Between Vibrations and Heat Transfer," <u>Wright Patterson AFB, Ohio Aeronautical Research Lab.</u> Dec. 1961, 36p. ARL-148, Part IV.
- 60. FAND, R. M. and OTHERS, "The Influence of Sound on Heat Transfer from a Cylinder in Crossflow," <u>Inter. J. of Heat and Mass Transfer</u>, <u>5</u>, July 1963, p. 571-596.

This paper reports the results of an experimental investigation of the influence of intense acoustic vibrations on the rate of heat transfer from a circular cylinder to air in crossflow. An excellent review of the literature concerning the effects of vibrations, induced by sound fields and mechanically, on natural convection from a simple shape to an infinite atmosphere is given.

- 61. FAND, R. M., "The Influence of Acoustical Vibrations on Convective Heat Transfer to Liquids," Office of Saline Water, Res. and Dev. Report No. 89, US dept. of Interior, PB181584 (1964).
- 62. FENSTER, S. K., VAN WYLEN, G. J. and J. A. CLARK, "Transient Pheomena Associated with the Pressurization of Liquid Nitrogen Boiling at Constant Heat Flux," <u>Advances in Cryogenic Engag</u>. <u>5</u>, pp. 226-234.
- 63. FULTZ, D. and Y. NAKAGAWA, <u>Proc. Roy. Soc.</u> (London), <u>A231</u>, p. 211 (1955). (Experimental data is reported for Mercury contained in a rotating vessel heated from below).
- 64. GERSHUNI, G. Z., "On Free Convection in Space Between Vertical Coaxial Cylinders," (in Russian), <u>Dokladi Akad, Nauk SSSR, N. S., 86</u>, 4, pp. 698-699, (Oct. 1952).
- 65. GOODY, R. M., "The Influence of Radiative Transfer on Cellular Convection," <u>J. Fluid Mechanics</u>, <u>1</u>, p. 424 (1956). (Free-convection studies in thin layers heated from below are reported.).
- 66. HAMMITT, F. G., "Heat and Mass Transfer in Closed, Vertical, Cylindrical Vessels with Internal Heat Sources for Homogeneous Reactors," PhD Thesis, Univ. of Mich. (Dec., 1957).
- 67. HAN, L. S., "Laminar Heat Transfer in Rectangular Channels," ASME Trans.

  J. Heat Transfer, 81, Series C, no. 2, pp. 121-128 (May, 1959).
- 68. HARDEN, D. G. and BOGGS, J. H., "Transient Flow Characteristics of Nat. Circulation Loop Operated in Critical Region," <u>Heat Transfer and Fluid Mechanics Institute-Porc</u>. <u>Preprints for Meeting June 10-12</u>, pp. 38-50 (1964).
- 69. HARJE, D. T., "Effect of Oscillating Flow on Heat Transfer in a Tube," <u>Progress Report No. 20-362, JPL</u>, Cal. Inst. of Tech. (Aug. 1958).
- 70. HARTNETT, J. P., W. E. WELCH and F. W. LARSEN, "Free Convection Heat Transfer to Water and Mercury in an Enclosed Cylindrical Tube,"

  Nuclear Engng. and Science Conference, preprint 27, Session XX, Chicago (March 17-21, 1958).
- 71. HARTNETT, J. P. and W. E. WELCH, "Experimental Studies of Free Convection Heat Transfer in a Vertical Tube with Uniform Heat Flux," Trns. ASME, 79, p. 1961 (1957).

Heat transfer rates were determined for water in a vertical tube closed at the bottom, with a length-radius ratio of 21. This uniform wall heat flux case was found to agree on the average with the constant wall temperature case. The local Nusselt number was found to increase rapidly at a critical Rayleigh number. Below this critical value, the results agree with the values for a vertical flat palte with uniform heat input.

- 72. HEATON, H. S., W. C. REYNOLDS, and W. M. KAYE, "Heat Transfer in Annular Passages. Simultaneous development of velocity and temperature fields in laminar flow," <u>International J. Heat Mass Transfer</u>, 7, no. 7, pp. 763-781 (July, 1964).
- 73. HELLUMS, J. S., "Finite-Difference Computation of Natural Convection Flow," PhD Thesis, Univ. of Mich. (Sept. 1960).
- 74. HENSHAW, D. H. and D. F. DAW, "Design of Cold Temperature Probes,"
  Nat. Aero. Establ. Cana. LR-184 (Jan. 1, 1954).
- 75. HOLMAN, J. P., H. E. GARTRELL AND F. E. SOEHNGEN, "A Study of Free Convection Boundary Layer Oscillations and Their Effects on Heat Transfer," WADC Tech. Report 59-3, Dec. 1959.
- 76. HOLMAN, J. P., and T. P. MOTT SMITH, "The Effects of High Constant Pressure Sound Fields on Free Convection Heat Transfer from a Horizontal Cylinder," WADC Tech. Note 58-352 ASTIA doc. no. 206906, Aero Res. Lab. (Dec. 1968).
- 77. HOLMAN, J. P., <u>J. Heat Transfer, C 82</u>, p. 393 (1960). Concerns a qualitative explanation of the change in heat transfer coefficients above a certain critical sound pressure.
- 78. HOLMAN, J. P., "The Mechanism of Sound Field Effects on Heat Transfer," J. of Heat Transfer, pp. 393-6 (Nov. 1960).

This paper attempts to explain the increase in heat transfer from a heated horizontal cylinder placed in a flow when a strong sound field is impressed on the flow, as the interaction of acoustical streaming with the boundary-layer flow.

It is noted here that at low sound intensity levels there is no effect on the heat transfer from the cylinder, whereas at high sound intensity levels there is an appreciable effect on the heat transfer from the cylinder. Several reasons are outlined in this paper to account for this increase in heat transfer.

- 79. ISAKOFF, S. E., "Analysis of Unsteady Flow Using Direct Electrical Analogs," <u>Ind. and Eng. Chem.</u>, <u>47</u>, no. 3, pp. 413-421 (March 1955).
- 80. IZUMI, R. "Natural Heat Convection Inside the Vertical Tube," <u>Proc. 6th Japan Nat. Congr. Appl. Mech. Univ. of Kyoto, Japan</u>, pp. 393-396 (Oct. 1956).

81. JACKSON, T. W., W. B. HARRISON and W. C. BOTELER, "Free Convection, Froced Convection, and Acoustic Vibrations in a Constant Temperature Vertical Tube," Trans. ASME J. Heat Transfer, 81, Series C, 68 (1959).

This paper concerns free convection, forced convection and acoustic vibrations in a constant temperature vertical tube.

The results from this paper were compared with the results of a previous study of free and forced convection in a constant temperature vertical tube without acoustic vibrations in an attempt to determine the effect of acoustic vibrations on heat transfer.

One important result noted was a critical sound level of 118 decibels. Below 118 decibels there was little effect of the acoustic vibrations on the heat transfer coefficient. Above 118 decibels there was a considerable effect of sound on the heat transfer and free convection forces seemed to be neglgible.

- 82. JACKSON, T. W., K. R. PURDY and C. C. OLIVER, "The Effects of Resonant Acoustic Vibrations on the Nusselt Numbers for a Constant Temperature Horizontal Tube," <u>Intern. Dev. in Heat Transfer</u>, <u>Boulder</u>, <u>Colo.</u> 1961 Part II, Sec. B, p. 483.
- 83. JOHNSON, N. R. and F. OSTERLE, "The Influence of Gradiant Temperature Fiedls on Thermocouple Measurements," <u>ASME-AICHE Heat Trans. Conf.</u>, <u>Univ. Park, Pa. Aig. 1957</u>, Pap. 57-HT-18, 20pp.
- 84. JONES, C. D. and D. J. MASSON, "An Interferometric Study of Free-Convection Heat Transfer from Enclosed Isothermal Surfaces," <u>Trans. ASME 77, 8</u>, pp. 1275-1281 (Nov. 1955).
- 85. KAYS, W. M. and A. L. LONDON, "Convective Heat Transfer and Flow-Fraction Behavior of Small Cylindrical Tubes--Circular and Rectangular Cross Sections," Trans. ASME, 74, 7, pp. 1179-1189 (Oct. 1952).
- 86. KESTIN, J., P.F. MARDER and H. E. WANG, "On Boundary Layers Associated with Oscillating Streams," Appl. Sci. Res. Section A., 10, no. 1 (1961).
- 87. KHLEBUTIN, G. N. and G. F. SHAILDUROV, "Heat Convection in a Vertical Annular Tube," (Russian) <u>Inzhen</u>. Fiz. Zh. 8, no. 1,pp. 3-7 (1965).

In this paper the natural convection of water and benzine ina vertical annular tube heated on one side and cooled on the other side is studied. It is stated that for constant temperature difference between the halves of the annulus, and circular motion of the liquid, that Nu=.125 Ra for Ra < 16,000. This study confirms this equation experimentally. It is also stated that for cellular liquid motion the Nusselt number is a function of the radius of the annulus and increases with the Rayleigh number more slowly than the above equation indicates.

88. KRASSOLD, H., "Warmeabgabe Von Zylindrischen Flussigkeitschieten bei Naturlicker Konvektion," <u>Frosch. Geb. Ingenieurw.</u>, <u>5</u>, pp. 136-191 (1943).

An experimental study of natural convection between concentric cylinders. The gap between the cylinders was filled with water, transofmer oil, or machine oil. Three diameter ratios were utilized; the ratio varying from 1.234 to 3. Gap thicknesses were 7, 20, and 40 mm. Prandtl numbers ranged from 7 to 4000 while the Grashof number range was .1 to  $10^{-8}$ .

89. KRAUS, A. D., "Heat Flow Theory," <u>Elec. Mfg., 63</u>, no. 4 pp. 123-42 (Apr. 1959).

A general discussion and determination of the basic equations for conduction, convection and radiation heat transfer. Dimensional analysis is used to establish the parameters and various 'numbers' involved in convection heat transfer. Solution of several emperical equations is presented using simulated experimental data.

90. KREITH, F., L. G. ROBERTS, J. A. SULLIVAN and S. N. SINHA, "Convection Heat Transfer and Flow Phenomena of Rotating Spheres," <u>Intern. J. of Heat and Mass Transfer</u>, 6, no. 10 pp. 881-95 (Oct. 1963).

The flow about and the convection heat transfer to or from a rotating sphere were investigated experimentally and theoretically. For Prandtl numbers between 4.0 and 217 and Reynolds numbers below 5  $\times$  10 $^4$  the average Nusselt number for cooling as well as heating was found to be in reasonably good agreement with the result of a theoretical analysis based on a solution of the boundary-layer equations in which the boundary-layer thickness around the sphere was assumed to be uniform. A detailed study of the flow by means of a hot wire and several flow visualization techniques is discussed.

- 91. KUBANSKII, P. N., "Intesifikatiya Teploobemna Ultrazvukom," <u>Teploenergetika</u>, no. 11, pp. 79-83 (Nov. 1962). (Effect of high amplitude acoustic oscillations on convective heat transfer.)
- 92. KUDRIASHEV, L. I. and TKACHEV, IU. A., "Investigation of the Effect of Body Vibrations on the Heat Transfer Coefficients in Conditions of Free Convection," Issledovanic uliianiia vibratsii Tela na Koeffitsient teplootdachi v usloviakh svobodnoi knovektsii, Aviatsionnaia Teknika, 8, no. 1, p. 54-72 (1965). (in Russian).
- 93. LARSON, M. B. and A. L. LONDON, "Study of Effects of Ultrasonic Vibrations on Convective Heat Transfer to Liquids," ASME Paper 62-HT-44 for meeting August 5-8, 1962, p. 16.

- 94. LARSON, M. B., "Study of Effects of Ultrasonic Vibrations on Convective Heat Transfer in Liquids," <u>Stanford University--Dept. of Mech. Engng.</u>
  <u>Tech. Report</u>, <u>48</u>, p. 102 (Sept. 30, 1960).
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## APPENDIX II

TEST CELL CONFIGURATION POSSIBILITIES

APPENDIX II

Test Cell Configuration possibilities (dimensions in inches)

Н	D	W	H/W	D/W
4	22	4.414	0.906	4.984
4	23	3.867	1.034	5.948
4	24	3.365	1.189	7.131
4	25	2.904	1.377	8.609
4	26	2.478	1.614	10.493
4	27	2.083	1.920	12.960
4	28	1.717	2.233	16.307
4	29	1.376	2.907	21.076
4	30			28.364
4	30	1.058	3.782	20.304
6	16	3.365	1.783	4.754
6	17	2.687	2.222	6.328
6	18	2.083	2.880	8.640
6	19	1.544	3.887	12.810
6	20	1.058	5.673	18.909
6	21	0.618	9.707	33.973
6	22	0.219	24.456	100.672
		0.22		
8	13	2.478	3.229	5.247
8	14	1.717	4.659	8.154
8	15	1.058	7.564	14.182
8	16	0.481	16.640	33.280
10	11	1.897	5.272	5.799
10	12	1.058	9.455	11.345
10	13	0.348	28.766	37.396
12	8	2.083	5.760	4.320
12	9	1.058	11.345	9.455
12	10	0.219	54.912	50.336
14	8	1.717	8.154	4.659
14	9	0.618	22.649	14.560
14	•	0.010	22.049	11.300
16	7	1.717	9.318	4.077
16	8	0.481	33.280	16.640
18	7	0.618	29.120	11.324
20	6	1.058	18.909	5.673
22	6	0.219	100.672	27.456
24	5	1.058	22.691	4.727